

# Advanced Functional Analysis

Fall Semester 2018

(First Semester 1397-1398)

**Code:** 2214175-01

**Credits:** 4

**Instructor:** Hossein Hosseini Giv ([giv@math.usb.ac.ir](mailto:giv@math.usb.ac.ir), [hossein.giv@gmail.com](mailto:hosseini.giv@gmail.com))

**Lecture times:** Sunday and Tuesday, 7:30-9:30 AM

**Classroom address:** Instructor's office at the Faculty of Mathematics

**Assessment Policy:** 40% midterm exam (04/10/1397), 60% final exam (25/10/1397)

**Textbook:** John B. Conway, *A Course in Functional Analysis*, Second Edition, Springer-Verlag New York, Inc., 1990.

## Course Contents

**1<sup>st</sup> week:** Compact operators

**2<sup>nd</sup> week:** Invariant subspaces: Preliminaries

**3<sup>rd</sup> week:** Invariant subspaces: Lomonosov's Theorem

**4<sup>th</sup> week:** Elements of Banach algebras

**5<sup>th</sup> week:** Ideals and quotients in Banach algebras

**6<sup>th</sup> week:** The spectrum

**7<sup>th</sup> week:** More on the spectrum

**8<sup>th</sup> week:** The Riesz functional calculus

**9<sup>th</sup> week:** Dependence of the spectrum on the algebra

**10<sup>th</sup> week:** The spectrum of a linear operator

**11<sup>th</sup> week:** Spectral theory of compact operators

**12<sup>th</sup> week:** Abelian Banach algebras

**13<sup>th</sup> week:** Elements of the theory of  $C^*$ -algebras

**14<sup>th</sup> week:** Abelian  $C^*$ -algebras

**15<sup>th</sup> week:** Positive elements of a  $C^*$ -algebra

**16<sup>th</sup> week:** The spectral theorem for normal operators