

Module title: Topics in Nonlinear Analysis

Lecturer: Dr Hamid Baghani

Module Subjects:

## Linear Spaces

1<sup>th</sup> week: Linear spaces, Normed spaces, Metric spaces

2<sup>th</sup> week: Convergence, Banach spaces, Completion of normed spaces

3<sup>th</sup> week: Inner product spaces, Orthogonality

4<sup>th</sup> week: Spaces of continuously differentiable functions, Holder spaces,  $L_p$  spaces, Compact sets

## Elementary Fixed Point Theorems

5<sup>th</sup> week: Results Based on Completeness

6<sup>th</sup>-7<sup>th</sup> weeks: Order-Theoretic Results

8<sup>th</sup>-9<sup>th</sup> weeks: Results Based on Convexity

10<sup>th</sup>-11<sup>th</sup> weeks: Further Results and Applications

## Theorem of Borsuk and Topological Transversality

12<sup>th</sup> week: Theorems of Brouwer and Borsuk

13<sup>th</sup>-14<sup>th</sup> weeks: Fixed Points for Compact Maps in Normed Linear Spaces

15<sup>th</sup> week: Compact and Completely Continuous Operators

16<sup>th</sup> week: Equation  $x = F(x)$ . The Leray-Schauder Principle and Birkhoff-Kellogg Theorem.