

**Reference:**

**Numerical Solution of Partial Differential Equations: Finite Difference Methods**

G. D. Smith

**Syllabus:**

**1. Introduction of PDEs**

Classification of PDEs , Elliptic, Hyperbolic, Parabolic

**2. Parabolic Equations: Finite Difference methods, Convergence and Stability**

Explicit Forward Euler method, Implicit Backward Euler Method, Crank-Nicolson, A weighted average approximation, Derivative boundary conditions, The local truncation error, consistency, convergence, Stability,

**3. Parabolic Equations**

Reduction To a system of ordinary differential equations, Finite difference approximation via the ordinary differential equations, Reduction of the local truncation error, use of three time-level difference equations, Deferred correction method, Linearization by Newton's method, Richtmyer's linearization method, A three time-level method

**4. Hyperbolic Equations**

First-order quasi-linear equations and characteristics, a method for numerical integration along a characteristic, Lax-Wendroff explicit method, Wendroff's implicit approximation, Second-order quasi-linear hyperbolic equations, Rectangular nets and finite-difference methods for second-order hyperbolic equations

**5. Elliptic Equations**

Derivative boundary conditions in heat-conduction problem, Finite-differences in polar coordinates, Formulae for derivatives near a curved boundary,